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## Part 2 - Beginning Algebra Summary

1. Numbers
1.1. Number Lines

| Number Lines | ( ) - If the point is not included <br> [ ]- If the point is included $\qquad$ - Shade areas where infinite points are included |  |
| :---: | :---: | :---: |
| Real Numbers | - Points on a number line <br> - Whole numbers, integers, rational and irrational numbers | $\triangleright 7,-7, \frac{7}{2}, \pi$ |
| Positive Infinity (Infinity) | - An unimaginably large positive number. (If you keep going to the right on a number line, you will never get there) |  |
| Negative Infinity | - An unimaginably small negative number. (If you keep going to the left on a number line, you will never get there) | $\stackrel{\longleftrightarrow}{-\infty}$ |

## Part 2 - Beginning Algebra Summary

### 1.2. Interval Notation

Interval Notation
(shortcut, instead of drawing a number line)

- 1st graph the answers on a number line, then write the interval notation by following your shading from left to right
- Always written: 1) Left enclosure symbol, 2) smallest number, 3) comma, 4) largest number, 5) right enclosure symbol
- Enclosure symbols
( ) - Does not include the point
[ ] - Includes the point
- Infinity can never be reached, so the enclosure symbol which surrounds it is an open parenthesis
Ex. $x=1$ " $x$ is equal to $1 "$


Ex. $x \neq 1$ " $x$ is not equal to 1 " . . . . . $\leftarrow_{-2-1} 0_{1}^{\mathrm{O}} \underset{2}{\longrightarrow}$
Ex. $x<1$ " $x$ is less than 1 ".


## Part 2 - Beginning Algebra Summary

## 2. Inequalities

| 2.1. Linear with 1 Variable |  |  |
| :---: | :---: | :---: |
| Standard Form | - $\quad a x+b<c \quad a x+b \leq c \quad a x+b>c \quad a x+b \geq c$ | $\triangleright 2 x+4>10$ |
| Solution | - A ray |  |
| Multiplication Property of Inequality | - When both sides of an inequality are multiplied or divided by a negative number, the direction of the inequality symbol must be reversed to form an equivalent inequality. | $\begin{aligned} \triangleright 4 & \leq-2 x \\ \frac{4}{-2} & \geq \frac{-2 x}{-2} \end{aligned}$ |
| Solving | 1. Same as Solving an Equation with 1 Variable (MA090), except when both sides are multiplied or divided by a negative number | $\begin{aligned} \text { Ex } 4 & \leq-2 x \\ \frac{4}{-2} & \geq \frac{-2 x}{-2} \\ -2 & \geq x \\ x & \leq-2 \end{aligned} \underset{-3-2-1}{\longrightarrow}$ |
|  | 2. Checking <br> - Plug solution(s) into the original equation. Should get a true inequality. <br> - Plug a number which is not a solution into the original equation. Shouldn't get a true inequality | $\begin{aligned} & \triangleright 4 \leq-2(-3) \\ & 4 \leq 6 \sqrt{ } \\ & \triangleright 4 \leq-2(0) \\ & 4 \leq 0 \times \end{aligned}$ |

## Part 2 - Beginning Algebra Summary

## 3. Linear Equations

### 3.1. The Cartesian Plane

| Rectangular Coordinate System | - Two number lines intersecting at the point 0 on each number line. <br> - X-AXIS - The horizontal number line <br> - Y-AXIS - The vertical number line <br> - ORIGIN - The point of intersection of the axes <br> - QUADRANTS - Four areas which the rectangular coordinate system is divided into <br> - ORDERED PAIR - A way of representing every point in the rectangular coordinate system $(x, y)$ | Quadrant II Quadrant I <br> Quadrant III Quadrant IV |
| :---: | :---: | :---: |
| Is an Ordered Pair a Solution? | - Yes, if the equation is a true statement when the variables are replaced by the values of the ordered pair | Ex $\quad x+2 y=7$ <br> $(1,3)$ is a solution because $1+2(3)=7$ |

## Part 2 - Beginning Algebra Summary

| 3.2. Graphing Lines |  |  |
| :---: | :---: | :---: |
| General | - Lines which intersect the $x$-axis contain the variable $x$ <br> - Lines which intersect the $y$-axis contain the variable $y$ <br> - Lines which intersect both axis contain $x$ and $y$ |  |
| Graphing by plotting random points | 1. Solve equation for $y$ <br> 2. Pick three easy $x$-values $\&$ compute the corresponding $y$-values <br> 3. Plot ordered pairs \& draw a line through them. (If they don't line up, you made a mistake) | $\begin{gathered} \triangleright x+2 y=7 \\ y=-\frac{x}{2}+\frac{7}{2} \end{gathered}$ |
| Graphing linear equations by using a point and a slope | 1. Plot the point <br> 2. Starting at the plotted point, vertically move the rise of the slope and horizontally move the run of the slope. Plot the resulting point <br> 3. Connect both points | $\begin{aligned} & \left.\left.\triangleright y=-\frac{1}{2}\right) x+\frac{7}{2}\right) \\ & \text { Point }=7 / 2 \\ & \text { Slope }=-1 / 2 \end{aligned}$  |

# Part 2 - Beginning Algebra Summary 

| 3.3. Intercepts and Slope |  |  |
| :---: | :---: | :---: |
| $x$-intercept $(x, 0)$ | - WHERE THE GRAPH CROSSES THE X-AXIS <br> - Let $y=0$ and solve for $x$ | Ex $\begin{aligned} & x+2 y=7 \\ & x+2(0)=7 \\ & x=7 \\ &(7,0) \end{aligned}$ |
| $\begin{aligned} & \hline \boldsymbol{y} \text {-intercept } \\ & (0, y) \end{aligned}$ | - WHERE THE GRAPH CROSSES THE Y-AXIS <br> - Let $x=0$ and solve for $y$ |  |
| Slope of a Line | - The slant of the line. <br> Let Point 1: $\mathrm{P}_{1}=\left(x_{1}, y_{1}\right) \&$ Point 2: $\mathrm{P}_{2}=\left(x_{2}, y_{2}\right)$ $\begin{aligned} m(\text { slope }) & =\frac{\text { rise }(\text { change in } \mathrm{y})}{\text { run }(\text { change in } \mathrm{x})} \\ & =\frac{y_{2}-y_{1}}{x_{2}-x_{1}} \end{aligned}$ | Ex Let $\mathrm{P}_{1}=(1,1), \mathrm{P}_{2}=(4,4)$ $m=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}=\frac{4-1}{4-1}=\underset{\rightarrow}{~}$ |
| Properties of Slope | - Positive Slope - Line goes up (from left to right). The greater the number, the steeper the slope <br> - NEGATIVE SLOPE - Line goes down (from left to right). The smaller the number (more negative), the steeper the slope. <br> - Horizontal line - Slope is 0 <br> - VERTICAL LINE - Slope is undefined <br> - PARALLEL LINES - Sanpe slope <br> - PERPENDICULAR LINES - The slope of one is the negative reciprocal of the other Ex: $m=-1 / 2$ is perpendicular to $m=2$ |  |
| Standard Form | - $\quad a x+b y=c$ <br> - $\quad x$ and $y$ are on the same side <br> - The equations contains no fractions and $a$ is positive | $\triangleright x+2 y=7$ |
| Slope-Intercept Form | - $y=m x+b$, where $m$ is the slope of the line, $\& b$ is the $y$-intercept <br> - " $y$ equals form"; "easy to graph form" | $\begin{aligned} & \triangleright \text { By solving } x+2 y=7 \text { for } y \\ & \qquad y=-\frac{x}{2}+\frac{7}{2} \end{aligned}$ |
| Point-Slope Form | - $y-y_{l}=m\left(x-x_{1}\right)$, where $m$ is the slope of the line \& $\left(x_{l}, y_{l}\right)$ is a point on the line <br> - Simplified, it can give you Standard Form or Slope-Intercept Form | $\begin{aligned} & \triangleright \operatorname{Using}(7,0) \text { and } m=-\frac{1}{2} \\ & y-0=-\frac{1}{2}(x-7) \end{aligned}$ |

# Part 2 - Beginning Algebra Summary 

| 3.4. Finding the Equation of a Line |  |  |
| :---: | :---: | :---: |
| If you have a horizontal line... | - The slope is zero <br> - $y=b$, where $b$ is the $y$-intercept | Ex. $y=3$ $\stackrel{\leftrightarrow}{\stackrel{\leftrightarrow}{\bullet}}$ |
| If you have a vertical line... | - The slope is undefined <br> - $x=c$, where $c$ is the $x$-intercept | Ex. $x=-3$ |
| If you have a slope \& y-intercept... | - Plug directly into Slope-Intercept Form | $\begin{aligned} & \text { Ex. } m=4 \& y \text {-intercept }(0,2) \\ & y=4 x+2 \\ & 2=4(0)+2 \sqrt{2} \end{aligned}$ |
| If you have a point \& a slope... | - Method 1 <br> 1. Use Point-Slope Form <br> 2. Work equation into Standard Form or Slope-Intercept Form | $\begin{aligned} & \text { Ex. point }(3,2) \& m=2 \\ & \begin{array}{l} y-2=2(x-3) \\ y-2=2 x-6 \\ y=2 x-4 \\ (2)=2(3)-4 \sqrt{ } \end{array} \end{aligned}$ |
|  | - Method 2 <br> 1. Plug the point into the SlopeIntercept Form and solve for $b$ <br> 2. Use values for $m$ and $b$ in the SlopeIntercept Form | $\begin{aligned} & \text { Ex. point }(3,2) \& m=2 \\ & y=m x+b \\ & \begin{array}{l} (2)=(2)(3)+b \\ 2=6+b \\ b=-4 \\ y=2 x-4 \\ (2)=2(3)-4 \sqrt{ } \end{array} \end{aligned}$  |
| If you have a point \& a line that it is parallel or perpendicular to... | 1. Determine the slope of the parallel or perpendicular line (e.g.. if it is parallel, it has the same slope) <br> 2. If the slope is undefined or 0 , draw a picture <br> 3. If the slope is a non-zero real number, go to If you have a point \& a slope... | Ex. point $(3,2) \&$ perpendicular to $x$-axis <br> $m=$ undefined $x=3$ <br> Ex. point $(3,2) \&$ perpendicular to $y=2 x-4$ $m=2$, so for perpendicular line $m=-1 / 2$ |
| If you have 2 points... | 1. Use the slope equation to determine the slope <br> 2. Go to If you have a point \& a slope... | $\begin{gathered} \text { Ex. }(0,0) \&(3,6) \\ \quad m=\frac{6-0}{3-0}=2 \end{gathered}$ |

## Part 2 - Beginning Algebra Summary

## 4. Systems of Linear Equations

| 4.1. Definitions |  |  |
| :---: | :---: | :---: |
| Type of Intersection | - IDENTICAL (I) - Same slope \& same y-intercept <br> - No SOLUTION (N) - Same slope \& different yintercept, the lines are parallel <br> - ONE POINT - Different slopes | Identical Consistent Dependent |
| Terminology | - CONSISTENT SYSTEM - The lines intersect at a point or are identical. System has at least 1 solution <br> - INCONSISTENT SYSTEM - The lines are parallel. System has no solution | No solution Inconsistent Independent $\leftarrow$ |
|  | - DEPENDENT EQUATIONS - The lines are identical. Infinite solutions <br> - INDEPENDENT EQUATIONS - The lines are different. One solution or no solutions | One point Consistent Independent |


| 4.2. Solving by Graphing |  |  |  |
| :--- | :--- | :--- | :---: |
| 1 | Graph both equations on the same Cartesian plane <br> The intersection of the graphs gives the common <br> solution(s). If the graphs intersect at a point, the <br> solution is an ordered pair. | $y=\frac{1}{2} x-1$ <br> $y=x-1$ |  |
| 2 | Check the solution in both original equations | $(0,-1)$ <br> $-1=\frac{1}{2}(0)-1$ <br> $-1=(0)-1$ |  |

## Part 2 - Beginning Algebra Summary

### 4.3. Solving by Substitution

1. Solve either equation for either variable. (pick the equation with the easiest variable to solve for)
2. Substitute the answer from step 1 into the other equation
3. Solve the equation resulting from step 2 to find the value of one variable *
4. Substitute the value form Step 3 in any equation containing both variables to find the value of the other variable.
5. Write the answer as an ordered pair
6. Check the solution in both original equations

Solve $\left\{\begin{array}{c}x-2 y=1 \\ 2 x-4=6 y\end{array}\right.$

1. $y=\frac{1-x}{-2}$
2. $2 x-4=\breve{-}_{6}^{-3}\left(\frac{1-x}{-2}\right)$
3. $2 x=-3+3 x+4$
$x=-1$
4. $y=\frac{1-(-1)}{-2}=-1$
5. $(-1,-1)$
6. $(-1)-2(-1)=1$
$1=1 \sqrt{ }$
$2(-1)-4=6(-1)$ $-6=-6 \sqrt{ }$
*If all variables disappear \& you end up with a true statement (e.g. $5=5$ ), then the lines are identical If all variables disappear $\&$ you end up with a false statement (e.g. $5=4$ ), then the lines are parallel

## Part 2 - Beginning Algebra Summary

### 4.4. Solving by Addition or Subtraction

1. Rewrite each equation in standard form $A x+B y=C$
2. If necessary, multiply one or both equations by a number so that the coefficients of one of the variables are opposites.
3. Add equations (One variable will be eliminated)*
4. Solve the equation resulting from step 3 to find the value of one variable.
5. Substitute the value form Step 4 in any equation containing both variables to find the value of the other variable.
6. Write the answer as an ordered pair
7. Check the solution in both original equations

Solve $\left\{\begin{array}{l}x-2 y=1 \\ 2 x-4=6 y\end{array}\right.$

1. $x-2 y=1$

$$
2 x-6 y=4
$$

2. Multiply both sides of the first equation by -2

$$
\begin{array}{rlrl} 
& & -2 x+4 y & =-2 \\
& 2 x-6 y & =4 \\
\hline \text { 3. } & -2 y & =2 \\
\text { 4. } & y & =-1 \\
\text { 5. } x-2(-1) & =1 \\
x & x & =-1
\end{array}
$$

6. $(-1,-1)$
7. $-2(-1)+4(-1)=-2$

$$
\begin{aligned}
-2 & =-2 \sqrt{ } \\
2(-1)-4 & =6(-1) \\
-6 & =-6 \sqrt{ }
\end{aligned}
$$

*If all variables disappear \& you end up with a true statement (e.g. $5=5$ ), then the lines are identical If all variables disappear $\&$ you end up with a false statement (e.g. $5=4$ ), then the lines are parallel

## 5. Word Problems

| 5.1. Solving |  |  |
| :---: | :---: | :---: |
|  | 1 Variable, 1 Equation Method | 2 Variables, 2 Equations Method |
| (1) Understand the <br> PROBLEM <br> - As you use information, eross it out or underline it. | In a recent election for mayor 800 people voted. Mr. Smith received three times as many votes as Mr. Jones. How many votes did each candidate receive? |  |
| (2) Define variables <br> - Create "Let" statement(s) <br> - The variables are usually what the problem is asking you to solve for | - Name what $x$ is (Can only be one thing. When in doubt, choose the smaller thing) <br> - Define everything else in terms of $x$ <br> Let $x=$ Number of votes Mr. J <br> $3 x=$ Number of votes Mr. S | Let $x=$ Number of votes Mr. S $y=$ Number of votes Mr. J |
| (3) Write the equation(s) <br> - You need as many equations as you have variables | $x+3 x=800$ | - Usually each sentence is an equation $\begin{aligned} x+y & =800 \\ x & =3 y \end{aligned}$ |
| (4) Solve the equation(s) | $\begin{aligned} 4 x & =800 \\ x & =200 \end{aligned}$ | $\begin{aligned} (3 y)+y & =800 \text { (Substitution) } \\ 4 y & =800 \\ y & =200 \end{aligned}$ |
| (5) ANSWER THE QUESTION <br> - Answer must include units! | - Go back to your "Let" statement <br> $200=$ Number of votes Mr. J <br> $600=$ Number of votes Mr. S | - Go back to your "Let" statement $200=$ Number of votes Mr. J <br> - Go back to your <br> "Equations" \& solve for remaining variable $\begin{aligned} x+(200) & =800 \\ x & =600 \end{aligned}$ <br> $600=$ Number of votes Mr. S |
| (6) CHECK <br> - Plug answers into equation(s) | $\begin{aligned} (200)+3(200) & =800 \\ 800 & =800 \sqrt{ } \end{aligned}$ | $\begin{aligned} (600)+(200) & =800 \\ 800 & =800 \sqrt{ } \\ (600) & =3(200) \\ 600 & =600 \sqrt{ } \end{aligned}$ |

## Part 2 - Beginning Algebra Summary

## 6. Polynomials

| 6.1. Definitions |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Term | - A constant, a variable, or a product of a constant and one or more variables raised to powers. |  |  |  |
| Polynomial | - A sum of terms which contains only whole number exponents and no variable in the denominator |  |  |  |
| Polynomial Name According to Number of Terms | Number of Terms | Polynomial Name | Examples |  |
|  | 1 | Monomial | $3 x$ |  |
|  | 2 | Binomial | $3 x+3$ |  |
|  | 3 | Trinomial | $x^{2}+2 x+1$ |  |
| Degree of a Polynomial Determines number of answers (x-intercepts) | 1. Express polynomial in simplified (expanded) form. <br> 2. Sum the powers of each variable in the terms. <br> 3. The degree of a polynomial is the highest degree of any of its terms |  |  |  |
| Polynomial Name According to Degree | Degree | Polynomial Name | Examples |  |
|  | 1 | Linear | $3 x$ |  |
|  | 2 | Quadratic | $3 x^{2}$ |  |
|  | 3 | Cubic | $3 x^{3}$ |  |
|  | 4 | Quartic | $3 x^{4} \quad 3 x^{3} y$ |  |

## Part 2 - Beginning Algebra Summary

| 6.2. Multiplication <br> Multiply each term of the first polynomial by each term of the second polynomial, and then combine like terms |  |
| :---: | :---: |
| Horizontal Method <br> - Can be used for any size polynomials | Ex: $(x-2)\left(x^{2}+5 x-1\right)$ |
| Vertical Method <br> - Can be used for any size polynomials. <br> - Similar to multiplying two numbers together | $\text { Ex: } \begin{array}{rrrr} (x-2)\left(x^{2}+5 x-1\right) \\ & x^{2} & 5 x & -1 \\ & & x & -2 \\ \hline & -2 x^{2} & -10 x & 2 \\ x^{3} & 5 x^{2} & -x & \\ \hline x^{3} & +3 x^{2} & -11 x & +2 \end{array}$ |
| FOIL Method <br> 1. May only be used when multiplying two binomials. First terms, Outer terms, Inner terms, Last terms | $\text { Ex: } \begin{aligned} & (x-2)(x-3) \\ = & \mathrm{F}^{\mathrm{F}} \bullet \\ = & x+x(-3)+(-2) x+(-2)(-3) \\ = & \left.x^{2}-3 x-2 x\right)+6 \\ = & x^{2}-5 x+6 \end{aligned}$ |

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|  | 6.3. Division <br> Dividing a Polynomial by a Monomial |
| :---: | :---: |
| Write Each Numerator Term over the Denominator Method $\frac{a+b+c}{d}=\frac{a}{d}+\frac{b}{d}+\frac{c}{d}$ | $\text { Ex: } \begin{aligned} & \frac{2 x+2}{4} \\ = & \frac{2 x}{4}+\frac{2}{4} \\ = & \frac{1}{2} x+\frac{1}{2} \end{aligned}$ |
| Factor Numerator and Cancel Method | $\text { Ex: } \begin{aligned} & \frac{2 x+2}{4} \\ = & \frac{2(x+1)}{4} \\ = & \frac{x+1}{2} \\ = & \frac{1}{2} x+\frac{1}{2} \end{aligned}$ |

# Part 2 - Beginning Algebra Summary 

## 7. Factoring

| Factoring | - Writing an expression as a product <br> - Numbers can be written as a product of primes. Polynomials can be written as a product of prime polynomials <br> - Useful to simplify rational expressions and to solve equations <br> - The opposite of multiplying | $\triangleright$ Factored $2(x+2)$ <br> $\triangleright$ Not factored $2 x+4$ $2 \cdot x+2 \cdot 2$ <br> tactoring $\triangleright 2 x+4=2(x+2)$ <br> Tnultiplying |
| :---: | :---: | :---: |
| GCF of a List of Integers | 1. Write each number as a product of prime numbers <br> 2. Identify the common prime factors <br> 3. The PRODUCT OF ALL COMMON PRIME FACTORS found in Step 2 is the GCF. If there are no common prime factors, the GCF is 1 | $\begin{aligned} & \triangleright \text { Find the GCF of } 18 \& 30 \\ & 18=2 \bullet 3 \bullet 3 \\ & 30=2 \bullet \cdot 3 \cdot 5 \\ & G C F=2 \bullet 3 \\ &=6 \end{aligned}$ |
| GCF of a List of Variables | - The variables raised to the smallest power in the list | $\begin{aligned} & \triangleright \text { Find the GCF of } x \& x^{2} \\ & \text { GCF }=x \end{aligned}$ |
| GCF of a List of Terms | - The product of the GCF of the numerical coefficients and the GCF of the variable factors | $\triangleright$ Find the GCF of $18 x \& 30 x^{2}$ GCF $=6 x$ |
| Factor by taking out the GCF | 1. Find the GCF of all terms <br> 2. Write the polynomial as a product by factoring out the GCF <br> 3. Apply the distributive property <br> 4. Check by multiplying | $\begin{aligned} \triangleright & -2 x^{2}+6 x^{3} \\ & =\left(-2 x^{2}\right) \square+\left(-2 x^{2}\right) \llbracket(-3 x) \\ & =-2 x^{2}(1-3 x) \\ & =-2 x^{2}+6 x^{3} \sqrt{ } \\ \triangleright & -x^{2}+1 \\ & =(-1)\left(x^{2}\right)+(-1) \llbracket(-1) \\ & =-1\left(x^{2}-1\right) \\ & =-x^{2}+1 \sqrt{ } \end{aligned}$ |

## Part 2 - Beginning Algebra Summary

### 7.2. 4 Terms <br> $\mathrm{a}+\mathrm{b}+\mathrm{c}+\mathrm{d}=(?+?)(?+?)$

- FACTOR BY GROUPING

1. Arrange terms so the $1^{\text {st }} 2$ terms have a common factor and the last 2 have a common factor
2. For each pair of terms, factor out the pair's GCF
3. If there is now a common binomial factor, factor it out
4. If there is no common binomial factor, begin again, rearranging the terms differently. If no rearrangement leads to a common binomial factor, the polynomial cannot be factored.
$\triangleright$ Factor 10ax-6xy-9y+15a
5. $10 a x+15 a-6 x y-9 y$
6. $5 a(2 x+3)-3 y(2 x+3)$
$(2 x+3)(5 a-3 y)$

## Part 2 - Beginning Algebra Summary

### 7.3. Trinomials: Leading Coefficient of 1 <br> $x^{2}+b x+c=(x+?)(x+?)$

- $\frac{\text { TRIAL \& ERROR }}{\swarrow}$ Product is $c>$
$(x+$ one number $)(x+$ other number $)$
$\wedge_{\text {Sum is } b} \rightarrow$

1. Place $x$ as the first term in each binomial, then determine whether addition or subtraction should follow the variable

$$
\begin{aligned}
& x^{2}+b x+c=(x+d)(x+e) \\
& x^{2}-b x+c=(x-d)(x-e) \\
& x^{2} \pm b x-c=(x+d)(x-e)
\end{aligned}
$$

2. Find all possible pairs of integers whose product is $c$
3. For each pair, test whether the sum is $b$
4. Check with FOIL $\sqrt{ }$

Ex: Factor $x^{2}+7 x+10$

1. $(x+)(x+)$
2. $2 \square 5=10$
$1 \square 10=10$
3. $2+5=7-\mathrm{YES}$
$1+10=11-\mathrm{NO}$
$(x+5)(x+2)$
4. $x^{2}+7 x+10 \vee$

# Part 2 －Beginning Algebra Summary 

## 7．4．Trinomials：All <br> $a x^{2}+b x+c=(? x+?)(? x+?)$

－METHOD 1 （trial \＆error）
1．Try various combinations of factors of $a x^{2}$ and $c$ until a middle term of $b x$ is obtained when checking．

2．Check with FOIL $\sqrt{ }$
－METHOD 2 （ $a c$ ，factor by grouping）
1．Identify $a, b$ ，and $c$
2．Find 2 ＂magic numbers＂whose product is $a c$ and whose sum is $b$ ．Factor trees can be very useful if you are having trouble finding the magic numbers （See MA090）

3．Rewrite $b x$ ，using the＂magic numbers＂found in Step 2
4．Factor by grouping
5．Check with FOIL $\sqrt{ }$
－METHOD 3 （quadratic formula）
1．Use the quadratic formula to find the $x$ values（or roots）

2．For each answer in step 1．，rewrite the equation so that it is equal to zero

3．Multiply the two expressions from step 2 ，and that is the expression in factored form．

4．Check with FOIL $\sqrt{ }$

Ex：Factor： $3 x^{2}+14 x-5$
Product is $3 x^{2}$ Product is -5


「ハブ
$15 x-x=14 x$（correct middle term）
Ex：Factor： $3 x^{2}+14 x-5$
1．$a=3$
$b=14$
$c=-5$
2．$a c=(3) \sqcup(-5)=-15$
$b=14$
$(15) \sqcup(-1)=-15 \vee$
$(15)+(-1)=14 \sqrt{ }$
＂magic numbers＂ $15,-1$
3． $3 x^{2}+15 x-x-5$
4． $3 x(x+5)-1(x+5)$
$(x+5)(3 x-1)$
Ex：Factor： $3 x^{2}+14 x-5$
1．$a=3$
$b=14$
$c=-5$
$x=\frac{-14 \pm \sqrt{14^{2}-4(3)(-5)}}{6}$
$x=\frac{1}{3},-5$

2．$x=\frac{1}{3}$
$x-\frac{1}{3}=0$
$3 x-1=0$
$x=-5$
$x+5 \Rightarrow 0$
3．$(3 x-1)(x+5)$

## Part 2 - Beginning Algebra Summary

### 7.5. $\quad$ Perfect Square Trinomials \& Binomials

| Perfect Square Trinomials $a^{2} \pm 2 a b+b^{2}$ | - Factors into perfect squares (a binomial squared) $\begin{aligned} & a^{2}+2 a b+b^{2}=(a+b)^{2} \\ & a^{2}-2 a b+b^{2}=(a-b)^{2} \end{aligned}$ | $\begin{gathered} \triangleright 9 x^{2}+24 x+16=(3 x)^{2}+2(3 x)(4)+(4)^{2} \\ =(3 x+4)^{2}(a=3 x, b=4) \\ \triangleright 9 x^{2}-24 x+16=(3 x)^{2}-2(3 x)(4)+(4)^{2} \\ =(3 x-4)^{2}(a=3 x, b=4) \end{gathered}$ |
| :---: | :---: | :---: |
| Difference of Squares $a^{2}-b^{2}$ | - Factors into the sum \& difference of two terms $a^{2}-b^{2}=(a+b)(a-b)$ | $\begin{aligned} \triangleright x^{2}-1 & =(x)^{2}-(1)^{2} \quad(a=x, b=1) \\ & =(x+1)(x-1) \end{aligned}$ |
| Sum of Squares $a^{2}+b^{2}$ | - Does not factor $a^{2}+b^{2}=$ Prime | $\triangleright x^{2}+1$ is prime |
| Difference of Cubes $a^{3}-b^{3}$ (MA103) | - $a^{3}-b^{3}=(a-b)\left(a^{2}+a b+b^{2}\right)$ | $\begin{aligned} \triangleright 8 x^{3}-27 & =(2 x)^{3}-(3)^{3}(a=2 x, b=3) \\ & =(2 x-3)\left(4 x^{2}+6 x+9\right) \end{aligned}$ |
| Sum of Cubes $a^{3}+b^{3}$ (MA103) | - $a^{3}+b^{3}=(a+b)\left(a^{2}-a b+b^{2}\right)$ | $\begin{aligned} \triangleright 8 x^{3}+27 & =(2 x)^{3}+(3)^{3}(a=2 x, b=3) \\ & =(2 x+3)\left(4 x^{2}-6 x+9\right) \end{aligned}$ |
| Prime Polynomials (P) | - Can not be factored | $\triangleright x^{2}+3 x+1$ is prime <br> $\triangleright x^{2}-3$ is prime |

## Part 2 - Beginning Algebra Summary

### 7.6. Steps to Follow

$\left.\begin{array}{|l|l|l|}\hline \text { 1. Put variable terms in descending order of degree with the } \\ \text { constant term last. }\end{array} \quad \begin{array}{c}\text { Ex. }-32+2 x^{4} \\ =2 x^{4}-32\end{array}\right]=2\left(x^{4}-16\right)$

## Part 2 - Beginning Algebra Summary

## 8. Quadratics

| 8.1. About |  |  |  |
| :--- | :--- | :--- | :--- |
| Standard Form | $\boxed{y} x^{2}+b x+c=0$ | $\triangleright x^{2}-3 x+2=0$ |  |
| Solutions | Has $n$ solutions, where $n$ is the <br> highest exponent | $\triangleright x^{3}-3 x^{2}+2 x=0$ (has 3 solutions) |  |


| 8.2. Graphing |  |  |
| :---: | :---: | :---: |
| Standard Form | $y=a x^{2}+b x+c$ <br> - $\quad a, b$, and $c$ are real constants | $\triangleright \mathrm{y}=x^{2}-9 x+20$ |
| Solution | - A parabola |  |
| Simple Form | $y=a x^{2}$ <br> - Vertex (high/low point) is $(0,0)$ <br> - Line of symmetry is $x=0$ <br> - The parabola opens up if $a>0$, down if $a<0$ | $\triangleright y=-4 x^{2}$ |
| Graph | 1. Plot $y$ value at vertex <br> 2. Plot $y$ value one unit to the left of the vertex <br> 3. Plot $y$ value one unit to the right of the vertex | $\triangleright y=-4 x^{2}$   |

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| 8.3. Solve by Factoring |  |  |
| :---: | :---: | :---: |
| Zero Factor Property | 1. If a product is 0 , then a factor is 0 | $\triangleright x y=0$ (either $x$ or $y$ must be zero) |
| Solve by Factoring | 1. Write the equation in standard form (equal 0) <br> 2. Factor <br> 3. Set each factor containing a variable equal to zero <br> 4. Solve the resulting equations | $\triangleright x^{2}-3 x+2=0$ <br> 1. $x(x-1)(x-2)=0$ <br> 2. $x=0, x-1=0, x-2=0$ <br> 3. $x=0,1,2$ |

## Part 2 - Beginning Algebra Summary

### 8.4. Solve with the Quadratic Equation

To solve a quadratic equation that is difficult or impossible to factor

1. Write the values for $a, b, \& c$ (if a term does not exist, the coefficient is 0)
2. Plug values into the
quadratic equation below:
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
3. Simplify solutions and usually leave them in their most exact form
(Negative radicand means no real solutions)

Ex Radicand is a perfect square

$$
\begin{aligned}
& x^{2}-3 x+2=0 \\
& a=1, b=(-3), c=2 \\
& x=\frac{-(-3) \pm \sqrt{(-3)^{2}-4(1)(2)}}{2(1)}=\frac{3 \pm \sqrt{1}}{2} \\
& \quad=2,1
\end{aligned}
$$

Ex Radicand breaks into "perfect square" and "leftovers"
$x^{2}+6 x-1=0$
$a=1, b=6, c=(-1)$
$x=\frac{-(6) \pm \sqrt{(6)^{2}-4(1)(-1)}}{2(1)}$
$=\frac{-6 \pm \sqrt{40}}{2}=\frac{-6 \pm 2 \sqrt{10}}{2}$
$=\frac{-6}{2} \pm \frac{2 \sqrt{10}}{2}=-3 \pm \sqrt{10}$
Ex Radicand is just "leftovers"

$$
\begin{aligned}
& 4 x^{2}-x-1=0 \\
& a=4, b=(-1), c=(-1) \\
& x
\end{aligned}=\frac{-(-1) \pm \sqrt{(-1)^{2}-4(4)(-1)}}{2(4)}, ~=\frac{1 \pm \sqrt{17}}{8}
$$

## Part 2 - Beginning Algebra Summary

## 9. Exponents

| 9.1. Computation Rules |  |  |
| :---: | :---: | :---: |
| Exponential notation <br> - Shorthand for repeated multiplication | base $\rightarrow x^{a}$ <exponent | $2^{3}=2 \cdot 2 \cdot 2=8$ |
| Multiplying common bases <br> - Add powers | $x^{a} \square x^{b}=x^{a+b}$ | $\begin{aligned} & 2^{2} \square^{3}=2^{2+3}=2^{5}=32 \\ & \left(3 x^{2}\right)(2 y)(4 x)=24 x^{3} y \end{aligned}$ |
| Dividing common bases <br> - Subtract powers | $\frac{x^{m}}{x^{n}}=x^{m-n}$ | $\frac{3^{5}}{3^{3}}=3^{5-3}=3^{2}=9$ |
| Raising a product to a power <br> - Raise each factor to the power | $\begin{aligned} & (x y)^{a}=x^{a} \square y^{a} \\ & \left(x^{m} y^{n}\right)^{a}=x^{m a} \square y^{n a} \end{aligned}$ | $\left(2 x^{3}\right)^{2}=2^{2} x^{6}=4 x^{6}$ |
| Raising a quotient to a power <br> - Raise the dividend and divisor to the power | $\left(\frac{x}{y}\right)^{n}=\frac{x^{n}}{y^{n}}$ | $\left(\frac{2}{z}\right)^{2}=\frac{2^{2}}{z^{2}}=\frac{4}{z^{2}}$ |
| Raising a power to a power <br> - Multiply powers | $\left(x^{a}\right)^{b}=x^{a \bullet b}$ | $\left(2^{3}\right)^{2}=2^{3 / 2}=2^{6}=64$ |
| Raising to the zero power <br> - One | $x^{0}=1$, when $x \neq 0$ | $6 x^{0}=(6)(1)=6$ |
| Raising to a negative power <br> - Reciprocal of positive power <br> - When simplifying, eliminate negative powers | $x^{-n}=\frac{1}{x^{n}}$ | $2^{3} \square^{-3}=\frac{2^{3}}{1} \frac{1}{2^{3}}=1$ |

## Part 2 - Beginning Algebra Summary

| 9.2. Scientific Notation |  |  |  |
| :---: | :---: | :---: | :---: |
| Scientific Notation | - Shorthand for writing very small and large numbers <br> - $a \bullet 10^{r}$, where $1 \leq a<10 \& r$ is an integer | $\left(1.2 \times 10^{2}\right)(1.2$ | $\left(1.2 \times 10^{2}\right)\left(1.2 \times 10^{3}\right)$ |
| Standard Form | - Long way of writing numbers | $120 \times 1200=144000$ |  |
| Standard Form to Scientific Notation | 1. Move the decimal point in the original number to the left or right so that there is one digit before the decimal point <br> 2. Count the number of decimal places the decimal point is moved in STEP 1 <br> - If the original number is 10 or greater, the count is positive <br> - If the original number is less than 1 , the count is negative <br> 3. Multiply the new number from STEP 1 by 10 raised to an exponent equal to the count found in STEP 2 | $\begin{aligned} & \hline 510 \\ & 5.10 \\ & +2 \\ & +2 \\ & 5.1 \times 10^{2} \end{aligned}$ | . 051 05.1 $-2$ $5.1 \times 10^{-2}$ |
| Scientific Notation to Standard Form | 1. Multiply numbers together | $\begin{aligned} & 5.1 \times 10^{2} \\ & =5.1 \times 100 \\ & =510 \end{aligned}$ | $\begin{aligned} & 5.1 \times 10^{-2} \\ & =5.1 \times \frac{1}{100} \\ & =.051 \end{aligned}$ |

## Part 2 - Beginning Algebra Summary

10. Radicals

| 10.1. Definitions |  |  |
| :---: | :---: | :---: |
| Roots | - Undoes raising to powers $\sqrt[2]{81}=9$ <br> because $9^{2}=81$ <br> index $\sqrt[2]{81} \kappa_{\text {radical }}$ $\uparrow$ radicand | $\triangleright \sqrt{81}=\sqrt[2]{81}=9$ <br> (The square root of 81 is 9 ) $\triangleright \sqrt{27}=\sqrt[3]{27}=3$ <br> (The cube root of 27 is 3 ) |
| Computation | - If $n$ IS AN EVEN POSITIVE INTEGER, then $\sqrt[n]{a^{n}}=\|a\|$ <br> The radical $\sqrt{ }$ represents only the non-negative square root of $a$. The $-\sqrt{ }$ represents the negative square root of $a$. <br> - IF $n$ IS AN ODD POSTIVIE INTEGER, then $\sqrt[n]{a^{n}}=a$ | $\begin{aligned} & \triangleright \sqrt{9}=\sqrt{3^{2}}=\|3\|=3 \\ & \triangleright \sqrt{(-3)^{2}}=\|-3\|=3 \\ & \triangleright \sqrt{(x+1)^{2}}=\|x+1\| \\ & \triangleright \sqrt{-9} \text { "Not a real number" } \\ & \triangleright-\sqrt{9}=-\sqrt{3^{2}}=-\|3\|=-3 \\ & \triangleright \sqrt{.09}=\|.3\|=.3 \quad(.3 \bullet .3=.09) \\ & \triangleright \sqrt{3} \approx\|1.73\| \approx 1.73 \text { (approximately) } \\ & \triangleright \sqrt[3]{27}=\sqrt[3]{3^{3}}=3 \\ & \triangleright \sqrt[3]{-27}=\sqrt[3]{(-3)^{3}}=-3 \end{aligned}$ |
| Notation: <br> Radical vs. <br> Rational Exponent | - The root of a number can be expressed with a radical or a rational exponent <br> - Rational exponents <br> - The numerator indicates the power to which the base is raised. <br> - The denominator indicates the index of the radical | $\begin{aligned} & \triangleright \sqrt[3]{27}=(27)^{1 / 3} \\ & \triangleright \sqrt[3]{27^{2}}=(\sqrt[3]{27})^{2}=27^{2 / 3}=\left(27^{1 / 3}\right)^{2} \\ & \triangleright \frac{1}{\sqrt[3]{27^{2}}}=\left(\frac{1}{\sqrt[3]{27}}\right)^{2}=27^{-2 / 3}=\left(27^{1 / 3}\right)^{-2} \end{aligned}$ <br> Note, it's usually easier to compute the root before the power |

## Part 2 - Beginning Algebra Summary

| 10.2. Computation Rules |  |  |
| :--- | :--- | :--- |
| Operations | • Roots are powers with fractional <br> exponents, thus power rules apply. | $\triangleright \sqrt[3]{-8 x^{3}}=\left(-8 x^{3}\right)^{1 / 3}$ <br> $=(-8)^{1 / 3}\left(x^{3}\right)^{1 / 3}=-2 x$ |
| Product Rule | $\sqrt[n]{a} \sqrt[n]{b}=\sqrt[n]{a b}$ | $\triangleright \sqrt{6} \sqrt{7}=\sqrt{42}$ |
| Quotient Rule | $\sqrt[n]{\frac{a}{b}}=\frac{\sqrt[n]{a}}{\sqrt[n]{b}}$, provided $\sqrt[n]{b} \neq 0$ | $\triangleright \sqrt{\frac{1}{25}}=\frac{\sqrt{1}}{\sqrt{25}}=\frac{1}{5}$ |

## Part 2 - Beginning Algebra Summary

## 11. Rationals

| 11.1. Simplifying Expressions |  |  |
| :---: | :---: | :---: |
| Rational Numbers | - Can be expressed as quotient of integers (fraction) where the denominator $\neq 0$ <br> - All integers are rational <br> - All "terminating" decimals are rational | $\begin{aligned} & \triangleright 0=0 / 1 \\ & \triangleright 4=4 / 1 \\ & \triangleright 4.25=17 / 4 \end{aligned}$ |
| Irrational Numbers | - Cannot be expressed as a quotient of integers. Is a non-terminating decimal | $\begin{aligned} & \triangleright \pi=3.141592654 \ldots \\ & \triangleright \sqrt{2}=1.414213562 \ldots \end{aligned}$ |
| Rational Expression | 1. An expression that can be written in the form $\frac{P}{Q}$, where $P$ and $Q$ are polynomials <br> 2. Denominator $\neq 0$ | $\triangleright \frac{x}{x+6}$, Find real numbers for which this expression is undefined: $x+6=0 ; x=-6$ |
| Simplifying Rational Expressions (factor) | 1. Completely factor the numerator and denominator <br> 2. Cancel factors which appear in both the numerator and denominator | $\begin{aligned} \triangleright & \text { Simplify } \frac{4 x+20}{x^{2}-25} \\ & =\frac{4(x+5)}{(x+5)(x-5)} \\ & =\frac{4}{x-5} \end{aligned}$ |

## Part 2 - Beginning Algebra Summary

### 11.2. Arithmetic Operations

| Multiplying/ <br> Dividing <br> Rational <br> Expressions <br> (multiply across) | 1. If it's a division problem, change it to a multiplication problem <br> 2. Factor \& simplify <br> 3. Multiply numerators and multiply denominators <br> 4. Write the product in simplest form | $\begin{aligned} \triangleright \text { Simplify } \frac{x}{x+6} \square \frac{3}{x} & =\frac{3 x}{x(x+6)} \\ & =\frac{3}{x+6} \end{aligned}$ |
| :---: | :---: | :---: |
| Adding/ Subtracting Rational Expressions (get common denominator) | 1. Factor \& simplify each term <br> 2. Find the LCD <br> * The LCD is the product of all unique factors, each raised to a power equal to the greatest number of times that it appears in any one factored denominator <br> 3. Rewrite each rational expression as an equivalent expression whose denominator is the LCD <br> 4. Add or subtract numerators and place the sum or difference over the common denominator <br> 5. Write the result in simplest form | $\begin{aligned} & \left.\left.\triangle \text { Simplify } \frac{x}{x+6}\right)+\frac{3}{6}\right) \\ & \quad=\frac{(6) x}{(6)(x+6)}+\frac{3(x+6)}{6(x+6)} \\ & \quad=\frac{6 x}{6(x+6)}+\frac{3 x+18}{6(x+6)} \\ & \quad=\frac{9 x+18}{6(x+6)} \\ & \quad=\frac{2^{3}(x+2)}{6^{2}(x+6)} \\ & =\frac{3 x+6}{2(x+6)} \end{aligned}$ |

## Part 2 - Beginning Algebra Summary

| 11.3. Solving Equations |  |  |
| :---: | :---: | :---: |
| Solving by Eliminating the Denominator | 1. Factor \& simplify each term <br> 2. Multiply both sides (all terms) by the LCD <br> 3. Remove any grouping symbols <br> 4. Solve <br> 5. Check answer in original equation. If it makes any of the denominators equal to 0 (undefined), it is not a solution | $\left.\begin{array}{l} \text { Solve } \frac{x}{x+6}+\frac{3}{x}=1 \\ \text { LCD }=x(x+6) \\ {[x(x+6)]\left[\frac{x}{x+6}+\frac{3}{x}\right]=[x(x+6)] 1} \\ {\left[\frac{x(x+6)}{1}\right]\left[\frac{x}{x+6}\right]+\left[\frac{x(x+6)}{1}\right]\left[\frac{3}{x}\right]=[x(x+6)] 1} \\ x(x)+3(x+6) \\ =1\left(x^{2}+6 x\right) \\ x^{2}+3 x+18 \end{array}\right)=x^{2}+6 x .\left[\begin{array}{rl} x & =6 \\ \text { Check } \frac{(6)}{(6)+6}+\frac{3}{(6)}=1 \\ \frac{1}{2}+\frac{1}{2} & =1 \sqrt{ } \end{array}\right.$ |
| Solving Proportions with the Cross Product $\frac{a}{b}=\frac{c}{d}$ | If your rational equation is a proportion, it's easier to use this shortcut <br> 1. Set the product of the diagonals equal to each other <br> 2. Solve <br> 3. Check | $\begin{aligned} 3(x-1) & =4 x \\ 3 x-3 & =4 x \\ x & =-3 \end{aligned}$ <br> Check $\frac{3}{4}=\frac{(-3)}{(-3)-1} \sqrt{ }$ |

## Part 2 - Beginning Algebra Summary

## 12. Summary

| 12.1. Formulas |  |  |
| :---: | :---: | :---: |
| Geometric | Triangle | - SUM OF ANGLES: Angle $1+$ Angle $2+$ Angle $3=180^{\circ}$ |
|  |  | - PYTHAGOREAN THEOREM: $a^{2}+b^{2}=c^{2}$ ( $a=\operatorname{leg}, b=\mathrm{leg}, c=$ hypotenuse) <br> $\sim$ The hypotenuse is the side opposite the right angle. It is always the longest side. |
| Other | Distance | - DISTANCE: $d=r t$ ( $r=$ rate, $t=$ time) |

Part 2 - Beginning Algebra Summary

| 12.2. Types of Equations |  |  |
| :---: | :---: | :---: |
|  | 1 Variable | 2 Variables |
| Linear Equations | $x-2=0$ <br> MA090 <br> Solution: 1 Point $\longleftrightarrow \underset{0}{1} \underset{2}{\longrightarrow}$ |  |
| Linear Inequalities | $\begin{array}{lll} \hline x-2<0 & & \text { page } \\ 4 \\ \text { Solution: Ray } & \underset{0}{\sim} \\ \end{array}$ | $y>x-2$ <br> Solution: $1 / 2$ plane |
| Systems of Linear Equations | $\left\{\begin{array}{l} x=7 \\ y=-5 \end{array}\right.$ <br> page 10 <br> Solution: 1 point, infinite points or no points | $\left\{\begin{array}{l} y=-x \\ y=x+2 \end{array}\right.$ <br> page <br> 10 <br> Solution: 1 point, infinite points or no points |
| Quadratic Equations | $\begin{array}{ll} \begin{array}{l} x^{2}+5 x+6=0 \\ 34 \\ \text { Solution: Usually } 2 \text { points } \\ \leftarrow \end{array} & \\ \xrightarrow[0]{*}-2 & 1 \\ \hline \end{array}$ |  |
| Higher Degree Polynomial Equations (cubic, quartic, etc.) | $x^{3}+5 x^{2}+6 x=0$ <br> Solution: Usually x points, where $x$ is the highest exponent | $y=x^{3}+5 x^{2}+6 x$ <br> Solution: Curve |
| Rational Equations | $\frac{x^{2}-1}{x+1}=1$ <br> page <br> 31 <br> Solution: Sometimes simplifies to a linear or quadratic equation | $y=-\frac{x^{2}-1}{x+1}+1$ <br> Solution: Sometimes simplifies to a linear or quadratic equation |

* To determine the equation type, simplify the equation. Occasionally all variables "cancel out".
- If the resulting equation is true (e.g. $5=5$ ), then all real numbers are solutions.
- If the resulting equation is false (e.g. $5=4$ ), then there are no solutions.


## Part 2 - Beginning Algebra Summary

### 12.3. Solve Any 1 Variable Equation



Make an equivalent, simpler equation

- If the equation contains fractions, eliminate the fractions (multiplying both sides by the LCD)
- If there is a common factor in each term, divide both sides of the equation by the common factor


Solve by "undoing" the equation

- Linear equations can by undone with the addition, subtraction, multiplication \& division equality properties
- Quadratics, of the form $(x+a)^{2}=b$, can be undone with the square root property

Write the equation in standard form

- Make one side equal to zero
- Put variable terms in descending order of degree with the constant term last


